

Introduction to EEG signal processing

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Content of the lecture

- Giving examples and illustrating the utility of the different methods
 1. Spectral distributions
 2. (TMS) evoked potential analysis
 1. Muscle artifact removal
 3. Source localization
 4. Brain computer interface

What to take home from this lecture?

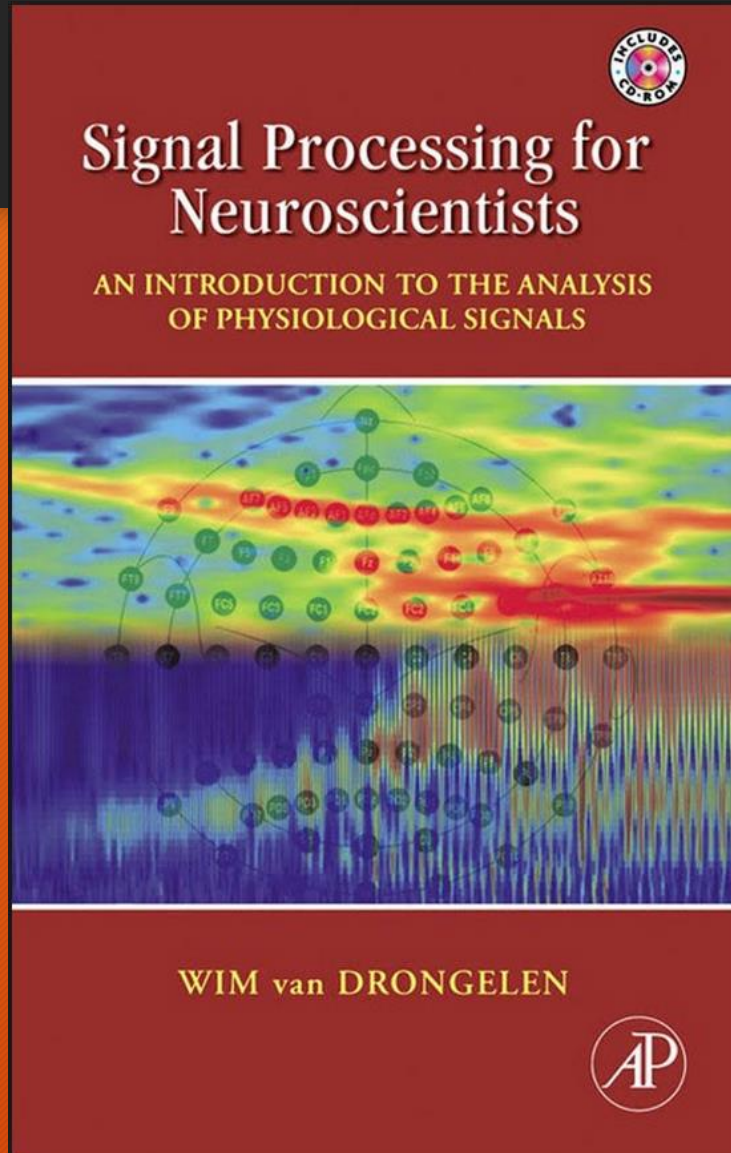
- Understand some basic signal processing ideas that apply to biosignals (and EEG in particular)
- What can you get out of a biosignal using these tools?

- Signal processing methods for continuous signal and evoked potentials (EP)
- EP's are time locked brain responses that are very weak (1 mikroVolts) compared to the background EEG activity (~tens of mikroVolts)
- You have to average up to 20 to 1000 EP's to get a visible signal

Basic components of biosignal processing

- Averaging
- Fourier analysis
- Filtering

- These are the tools used in clinical patient work



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Example #1 Spectral distributions

- Problem: How to view long periods of EEG data in order to detect relevant changes in patient's state
- Goal: Time-frequency plot of the power of EEG - finger print of the brain dynamics (short and/or time-locked dynamics)

Spectral analysis

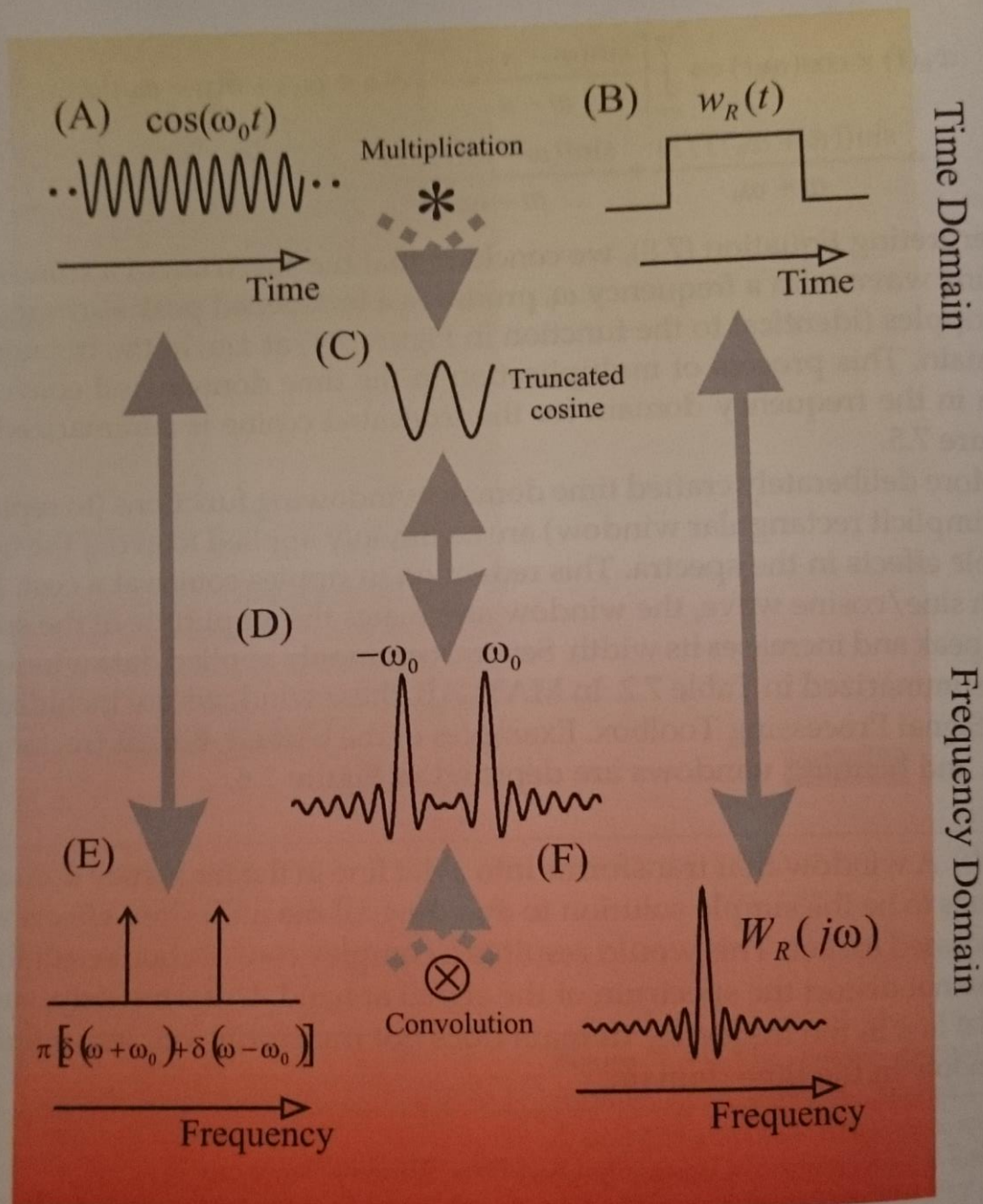
- Fourier theorem: any signal can be expressed as an infinite sum of sine and cosine components
- Theoretically straightforward but biosignals have characteristics that complicate the analysis
- Namely, they are not stationary and contain periodic and non-periodic components
- Solution is to analyse small periods of EEG and make an assumption that the signal is *approximately* stationary in the time period

Fourier theorem

$$\hat{f}(\xi) = \int_{-\infty}^{\infty} f(x) e^{-2\pi i x \xi} dx,$$

$$f(x) = \int_{-\infty}^{\infty} \hat{f}(\xi) e^{2\pi i x \xi} d\xi,$$

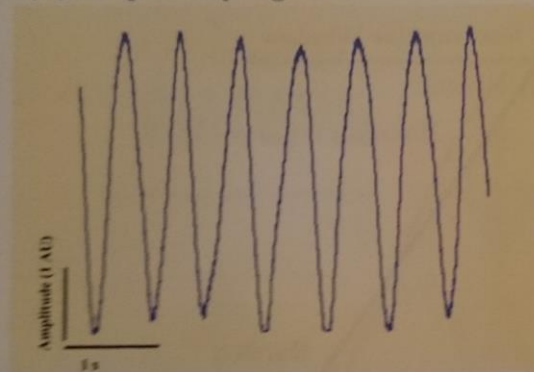
- Uncertainty relation between time (x) and frequency (ξ)
- Generally speaking, the more concentrated $f(x)$ is, the more spread out its Fourier transform $\hat{f}(\xi)$ must be.
- Assumes stationarity of the signal



Overview of the Fourier transform of a truncated cosine wave. A theoretically infinite cosine wave (A) multiplied by a rectangular window (B) generates truncated wave C. The Fourier transform of the cosine and the window in the frequency domain are shown in E and (F). The transform of the truncated cosine is the convolution of its components, shown in (D).

- Fourier analysis applied to a non stationary signal (EEG) creates ripple artefacts as shown in previous figure
- Artefactual harmonic frequency components
- Not all peaks in a spectrum correspond to actual physiological events

(A) Respiratory Signal



(B) Amplitude Spectrum

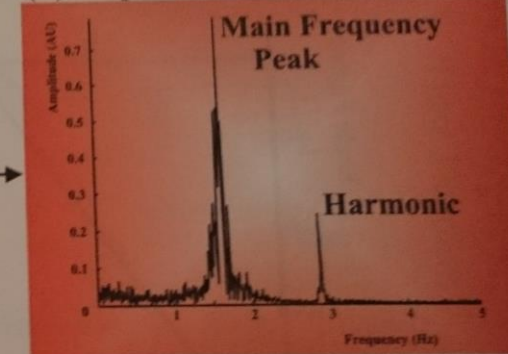
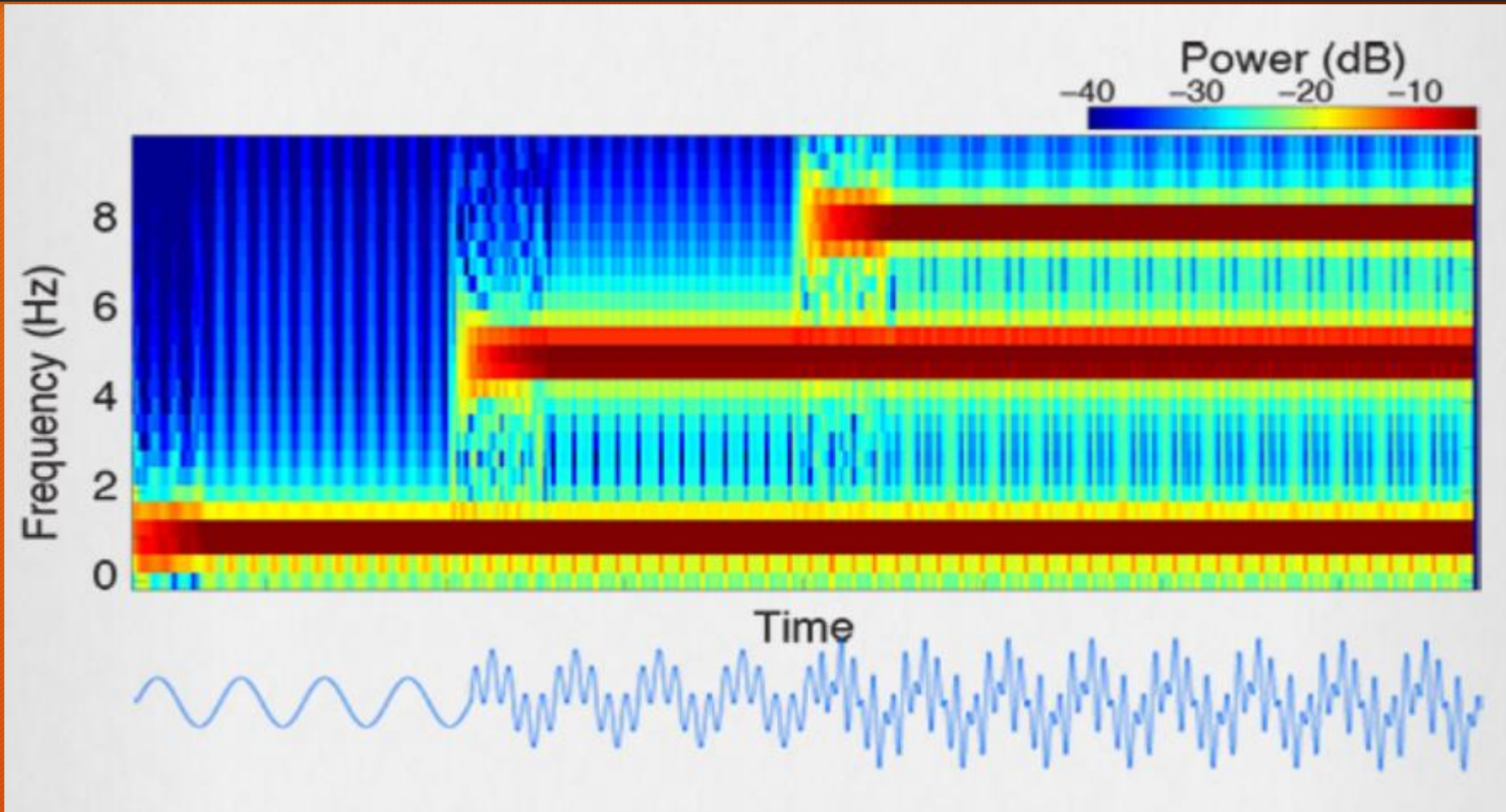
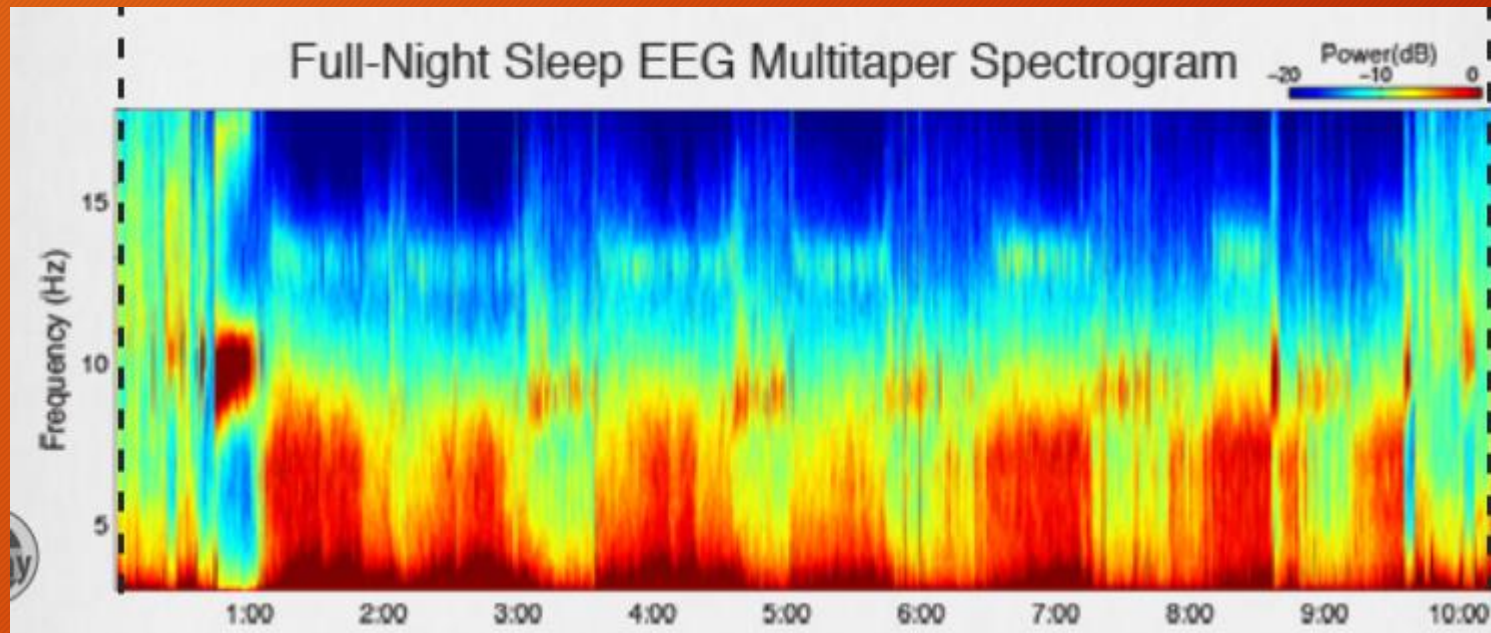


Figure 7.7 Frequency analysis of a respiratory signal from a human neonate. An epoch of the time domain signal is shown in (A) and the amplitude spectrum in (B). Clearly the main peak ~ 1.5 Hz shows the respiratory frequency, whereas the peak close to 3 Hz is a harmonic due to the imperfect sinusoidal signal. The respiration signal, sampled at 1 kHz, is available on the CD (respiration.mat).

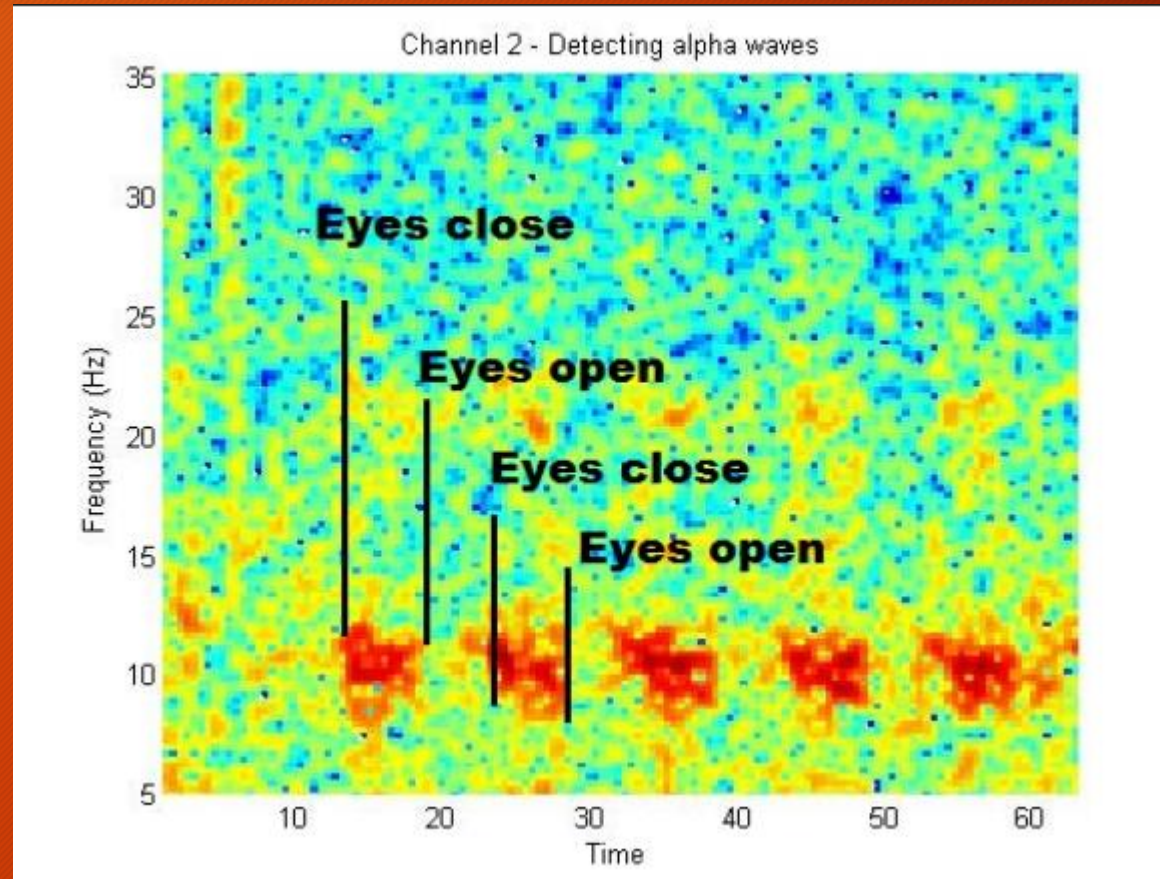
Spectrogram



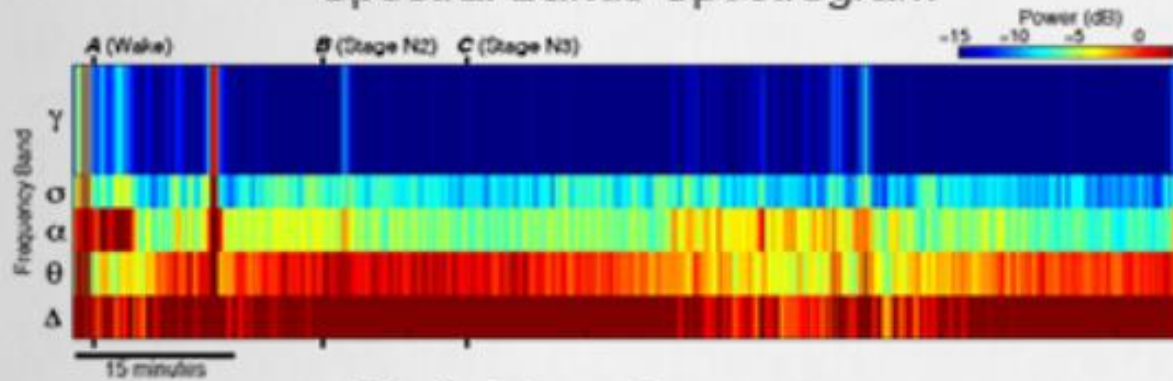
- 10 hours of EEG data at a glance
- Easy to detect which frequencies dominate the data
- Periodic activity



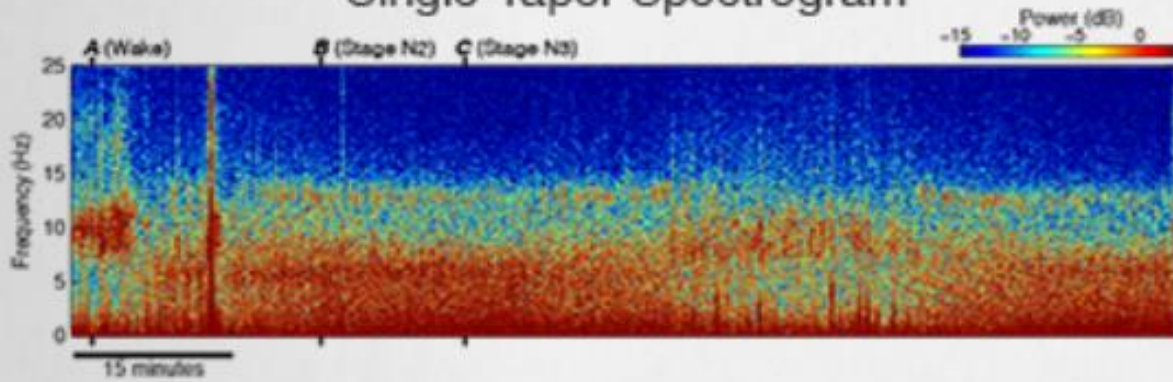
Spectrogram



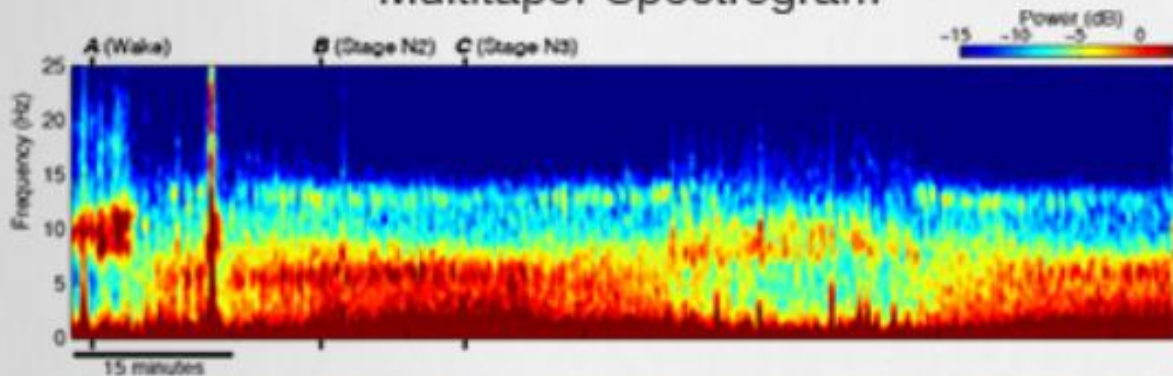
Spectral Bands Spectrogram



Single-Taper Spectrogram



Multitaper Spectrogram



- Taper function is used to truncate the data
- Shape of taper function affects the data quality
- Multitaper has multiple taper functions applied and averaged to increase the resolution

When using spectrograms

- Matlab (EEGLab)
- Determine at what time periods the signal can be said to be stationary
- Determine what you need the frequency resolution to be
- Trade-off between frequency and time resolution

What are spectrographs used for?

- Effective way to analyze complex oscillatory data
- Long-time EEG monitoring in the ICU
- Sleep staging
- Classifying brain responses for e.g. test subject reading/thinking different words - Mind reading?!

Example #2 Evoked potential data analysis

- Evoked potentials are brain responses to a stimulus
- Transcranial magnetic stimulation (TMS)
- Other ways to elicit an evoked potential,
 - E.g. auditory or visual stimulus
- Principal for all evoked potential (EP) data processing is the same



Example #2 Evoked potential data analysis

EEG responses to magnetic stimulation

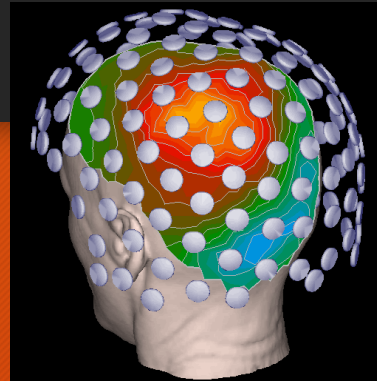
Goal: To probe cortical dynamics, i.e., obtain time-amplitude description of the brain's response to a magnetic stimulus



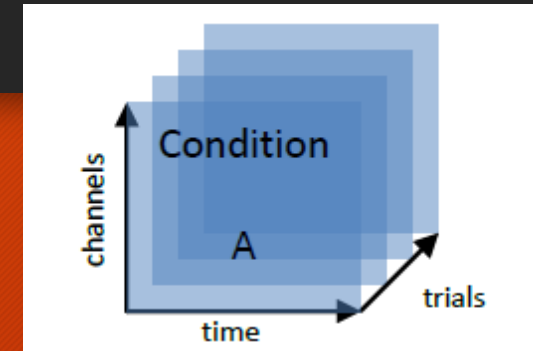
Structure of the Data

Structure of TMS-EEG data

- 1 TMS pulse
- EEG recording
- n TMS pulses
- n EEG recordings

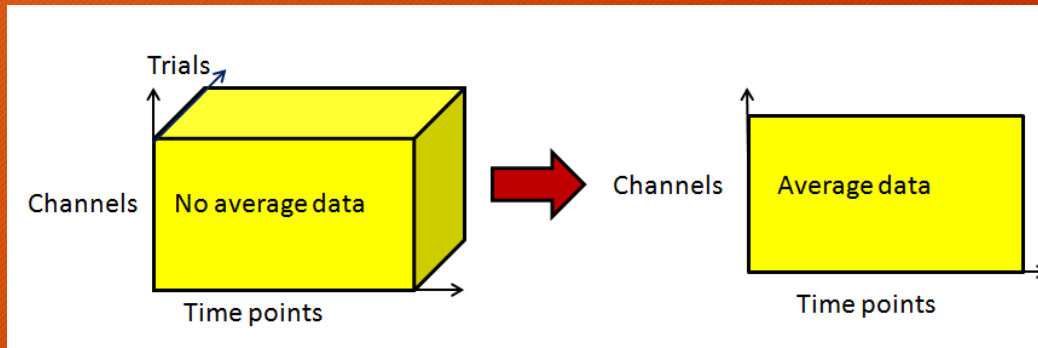


3-Dimensional data

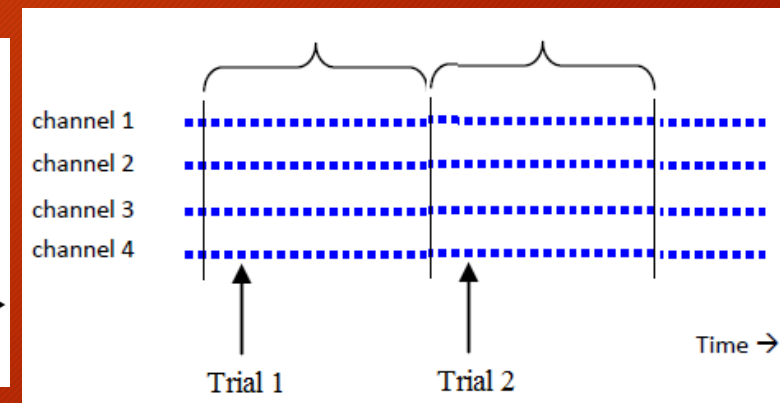


2-Dimensional data

Average over trials



Concatenation of the trials



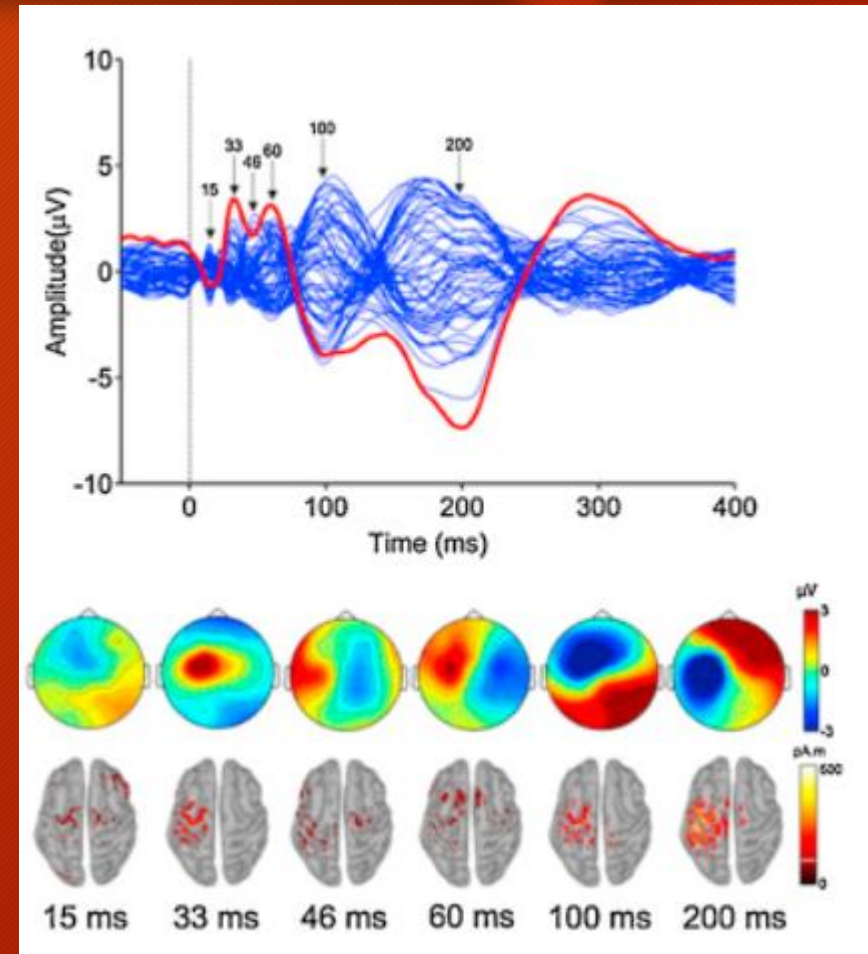
TMS evoked potential (TEP)

Examples of TMS-evoked potentials following stimulation over the [motor cortex \(M1\)](#). At the top butterfly plots from all electrodes with timing of peaks indicated by arrows (note different amplitude scales between the two plots). The red line indicates the electrode under the coil (C3 for M1). In the bottom half topographic maps of voltage distributions over time across the scalp (top) and following source reconstruction (bottom) for each peak.

A. T. Hill et al, "TMS-EEG: A window into the neurophysiological effects of transcranial electrical stimulation in non-motor brain regions"

[Neuroscience & Biobehavioral Reviews](#)

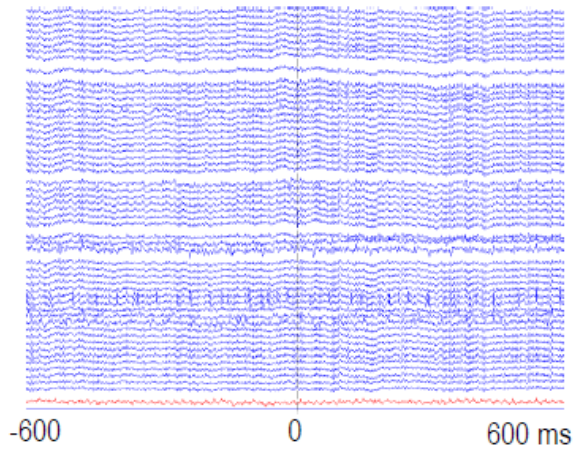
[Volume 64](#), May 2016, Pages 175-184



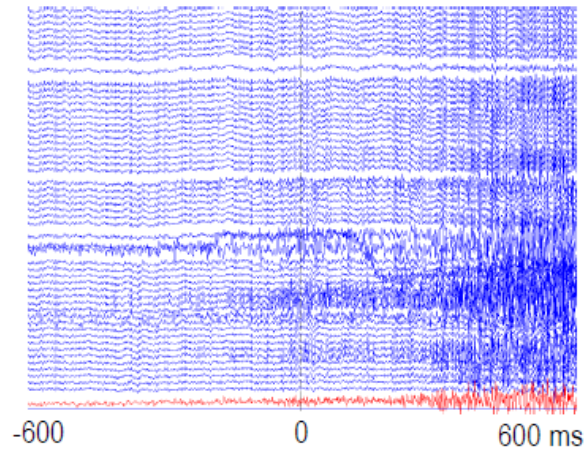
Signal analysis processing of TMS-evoked EEG

1. Visual inspection of trials: you can reject bad trials if something is wrong...

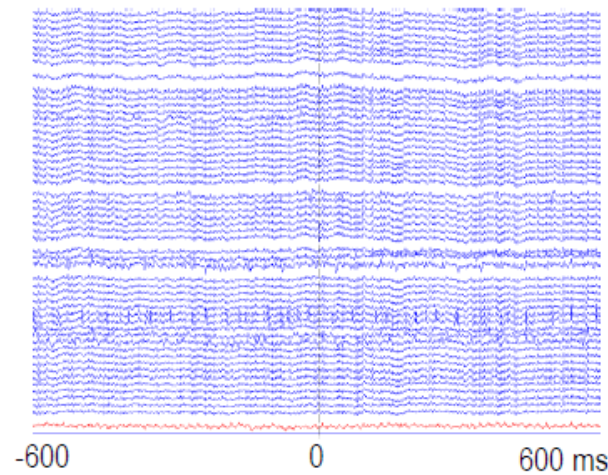
Good trial



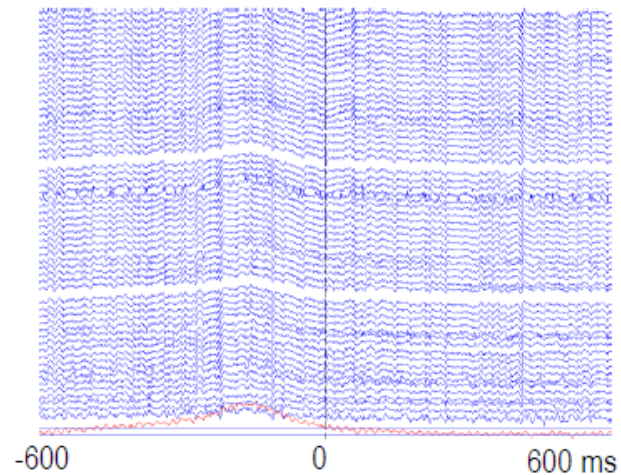
Bad trial: muscle activity



Good trial

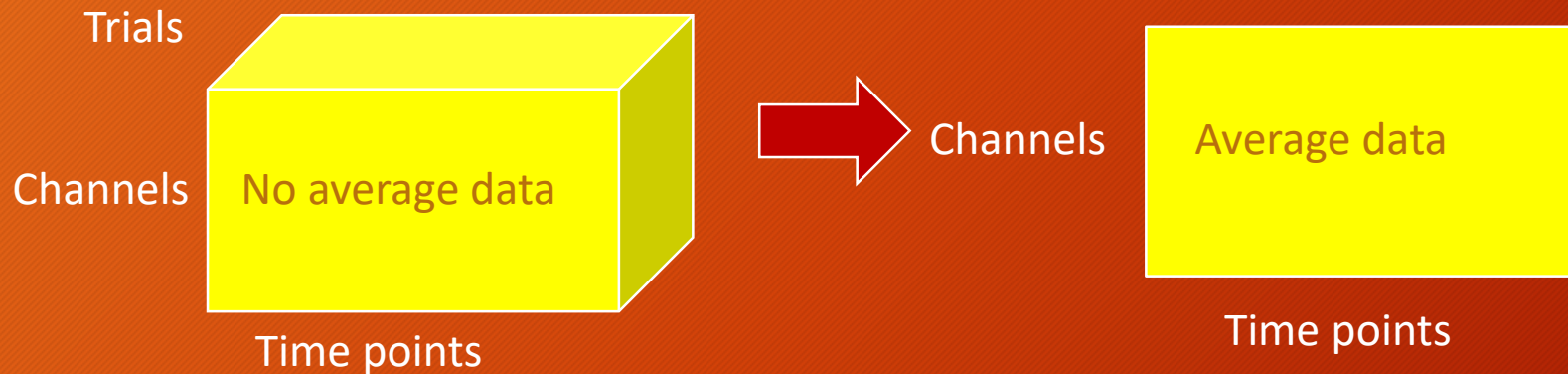


Bad trial: blink activity



Preprocessing steps:

2. Averaging the data



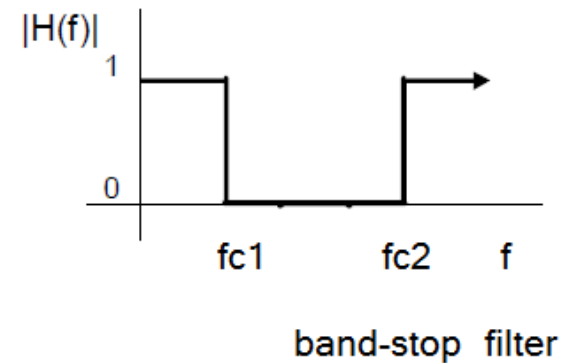
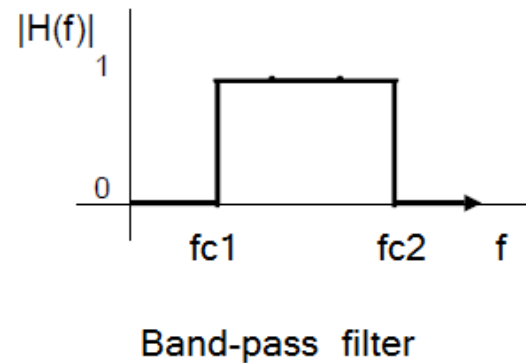
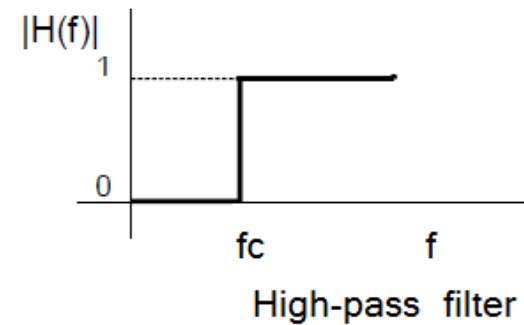
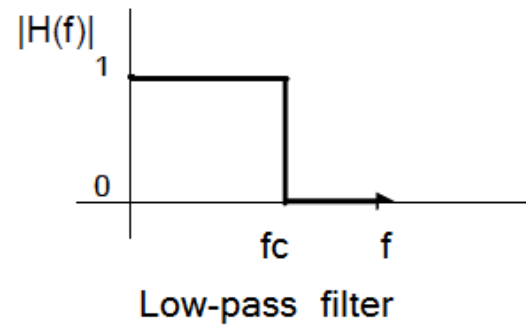
3. Removing bad channels: poor electrodes connection, disconnected channels

4. Filtering

Filtering

Filtering is the process of keeping components of the signal with certain desired frequencies and removing components of the signal with certain undesired frequencies.

24



f_c = cutoff frequency

4. Referencing the average potential over the channels

$$\mathbf{X}_z(j, t) = \mathbf{X}_r(j, t) - \frac{1}{M} \sum_{k=1}^M \mathbf{X}_r(k, t)$$

5. Time centering (baseline correction)

$$\mathbf{X}_c(j, t) = \mathbf{X}_z(j, t) - \frac{1}{N} \sum_{s=1}^N \mathbf{X}_z(k, s)$$

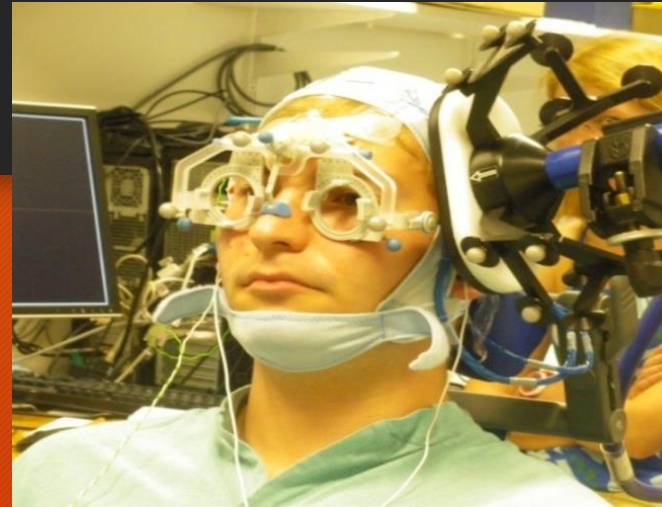
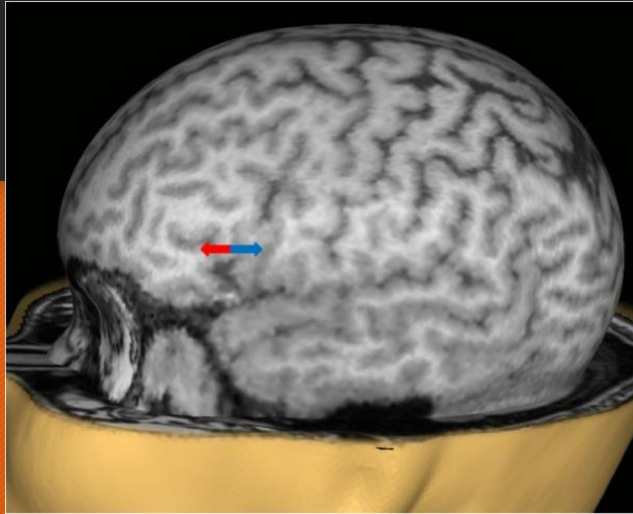
Independent component analysis

6. Artefact removal with ICA

Particularly good for removing muscle artefact that is very hard to avoid with magnetic stimulation

Muscle artifacts in Broca's area

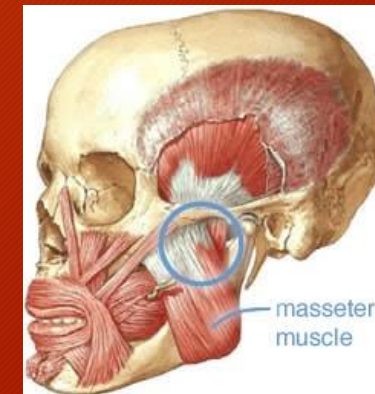
Muscle artifacts



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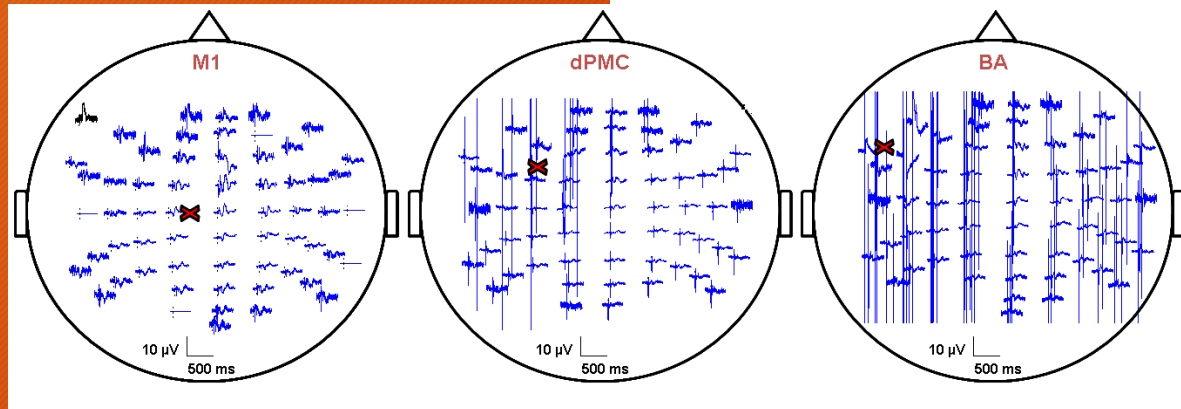
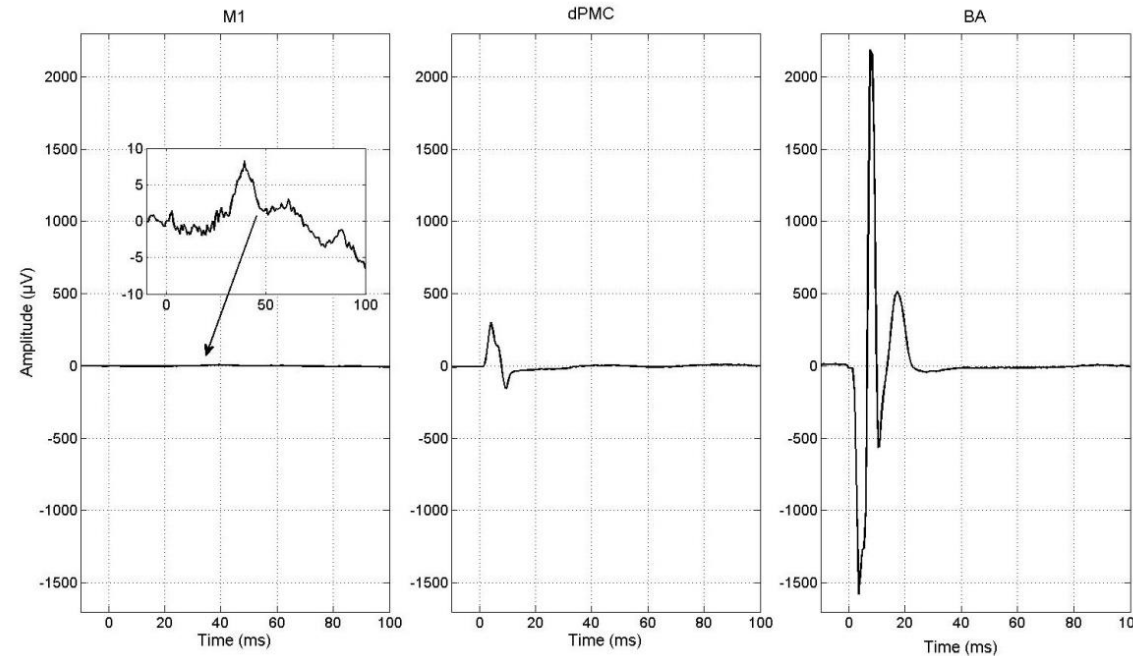
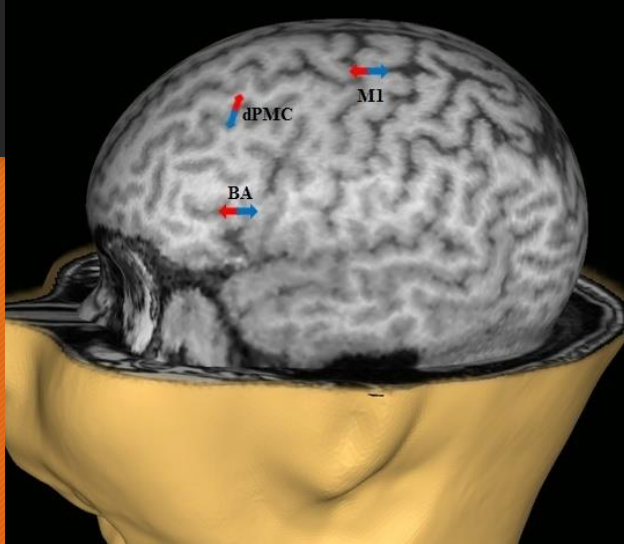
Muscle artifacts:

1. Are most prominent when lateral areas of the head or areas near the neck or forehead are stimulated.
2. **Temporal** and **frontal muscles**, and in some stimulation positions, **masseter muscle** (one of the muscle of mastication) are the most likely to be activated.



TMS-evoked EEG data from Broca's area

Muscle artifacts:

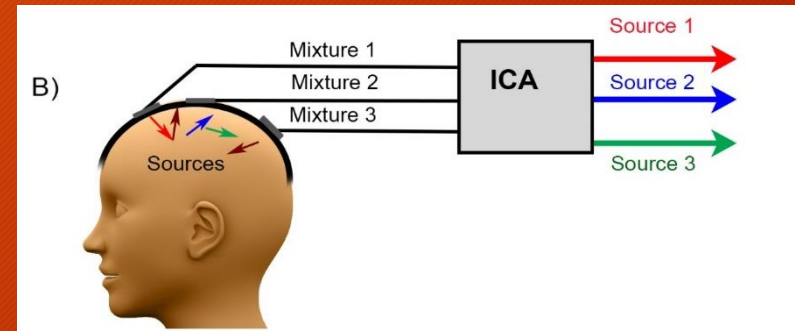
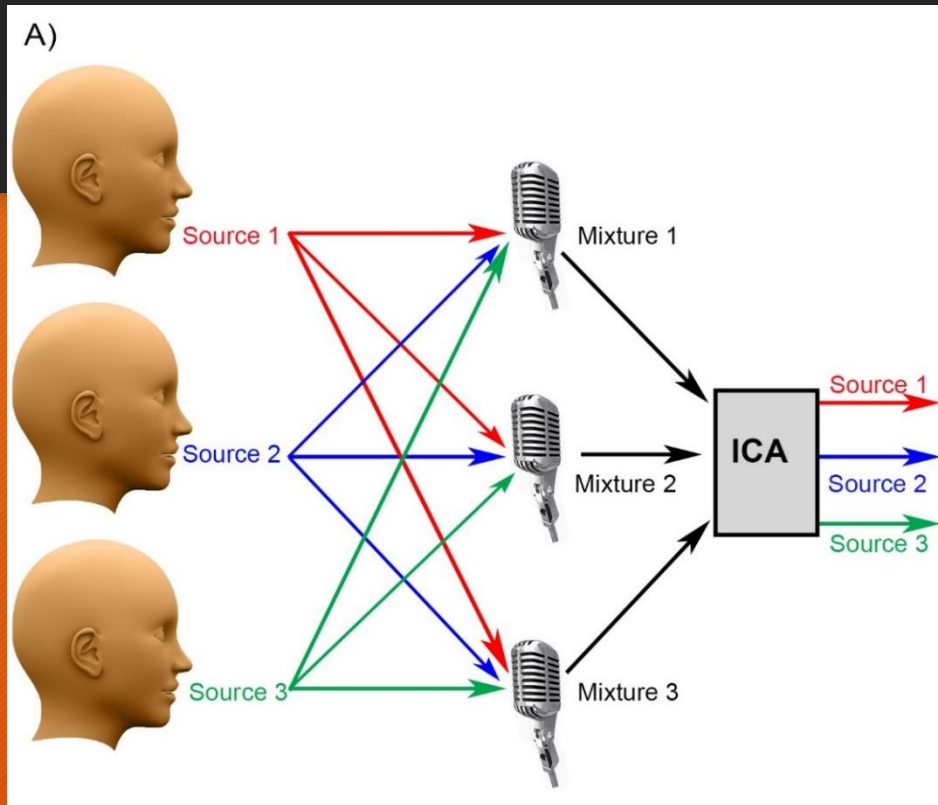


Muscle artifacts:

1. They mask the brain signals. 2-3 orders of magnitude larger than brain signals.

2. They last for tens of milliseconds (30 ms)

Principle of ICA



The EEG recordings are composed of mixed signals, *i.e.*, **brain responses** and **non-brain sources**, such as muscle artifacts.

Independent component analysis (ICA)

- ICA is a method for finding underlying factors or components from *multivariate* (multidimensional) statistical data.

- ICA looks for components that are *statistically independent and non-Gaussian*

is an $M \times T$ matrix.

- Matrix of recorded data.

$$\mathbf{X} = \mathbf{AS} = \sum_{j=1}^n a_j s_j$$

is an $M \times n$ mixing matrix.

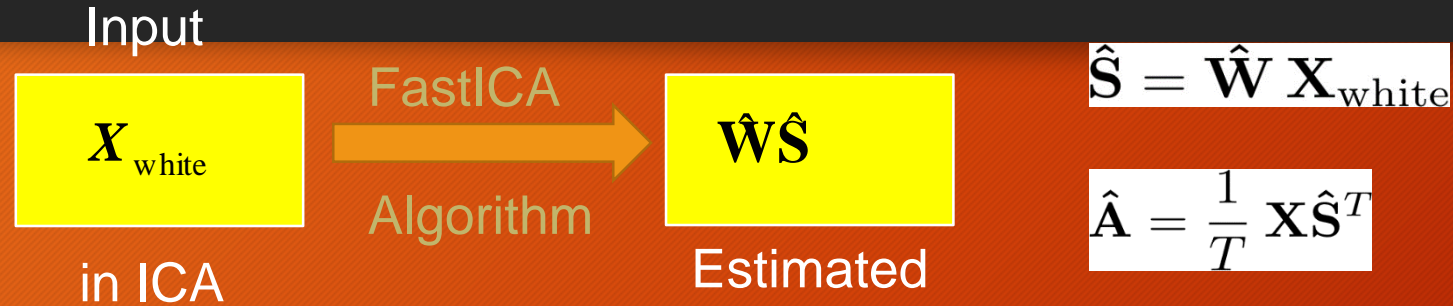
- Their columns are the topographies of the n latent sources.

is an $n \times T$ time-courses matrix.

- Their rows are the time-courses (amplitudes) of the latent variables.

Independent component analysis (ICA)

- Applying ICA requires additional steps (compressing extra dimensions, whitening) that we will not go into detail...

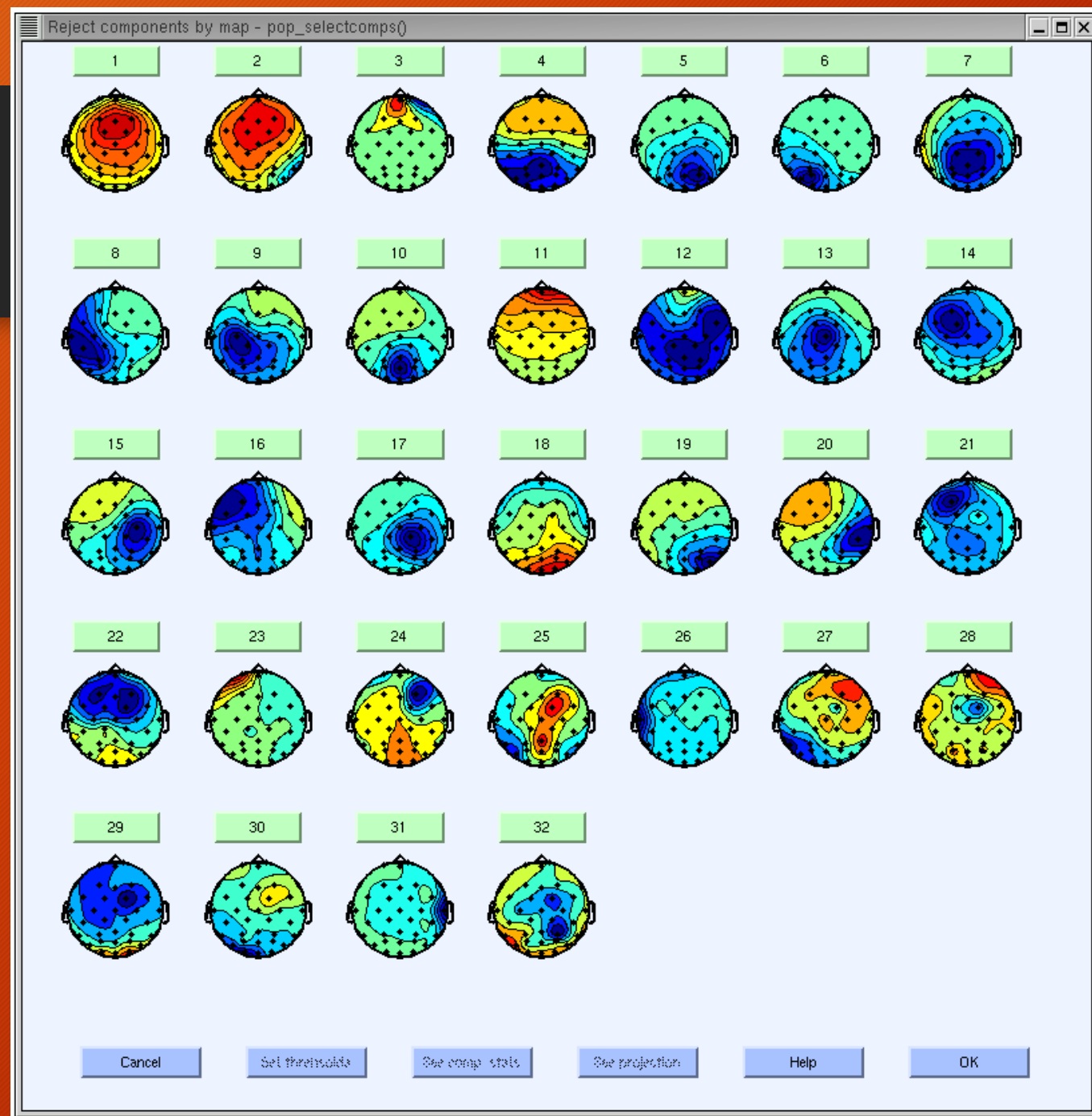


Preprocessing steps:

- 1) Removing bad channels and trials
- 2) Set the zero potential level or reference potential
- 3) Centering (zero mean)
- 4) Compressing extra dimensions
- 5) Whitening

Results of ICA

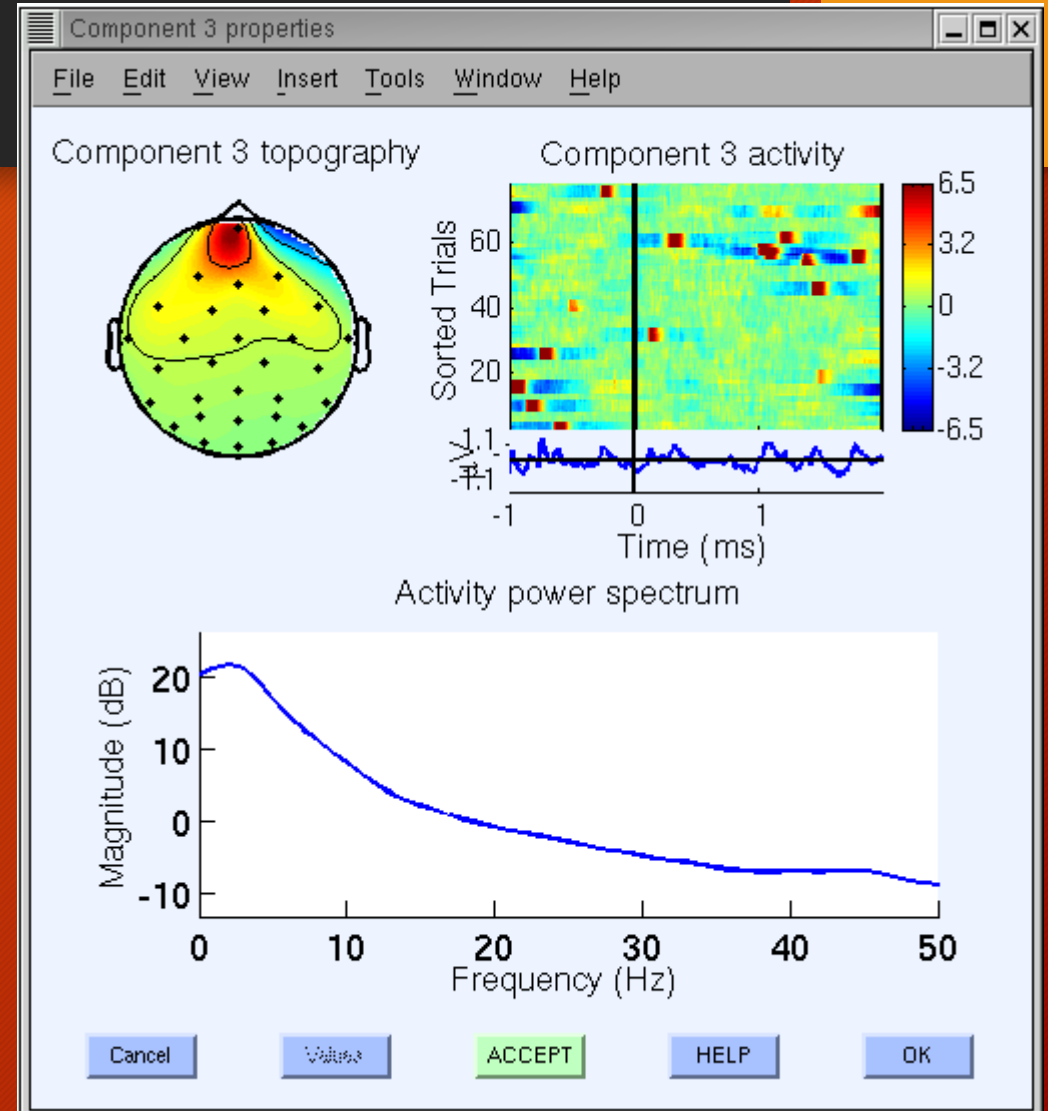
- 32 independent components
- Some are EEG components, some are artefacts



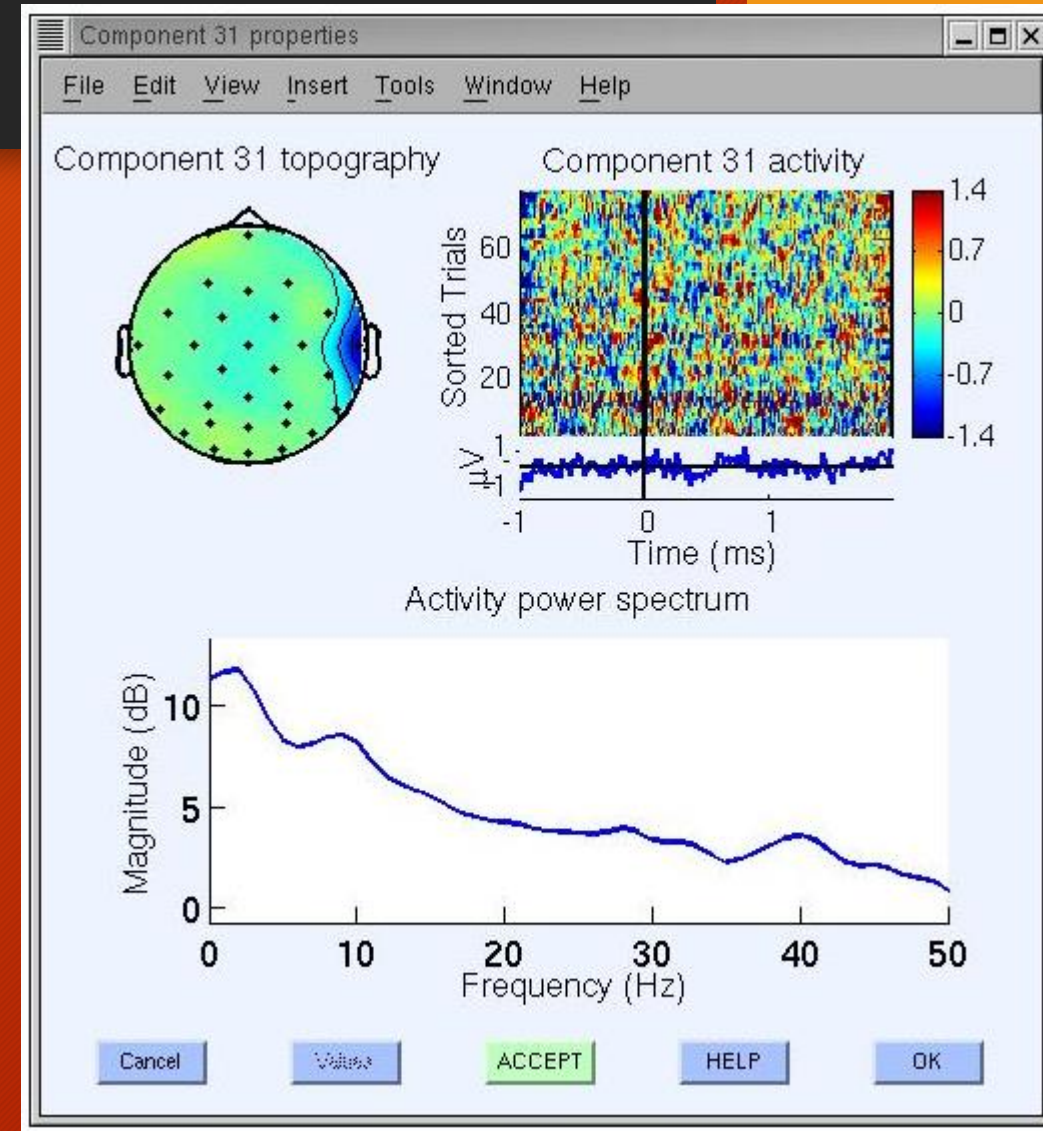
- To help with deciding which component to remove, look at additional data

- Eye movement

- Topoplot frontal
- Periodicity in spectrum

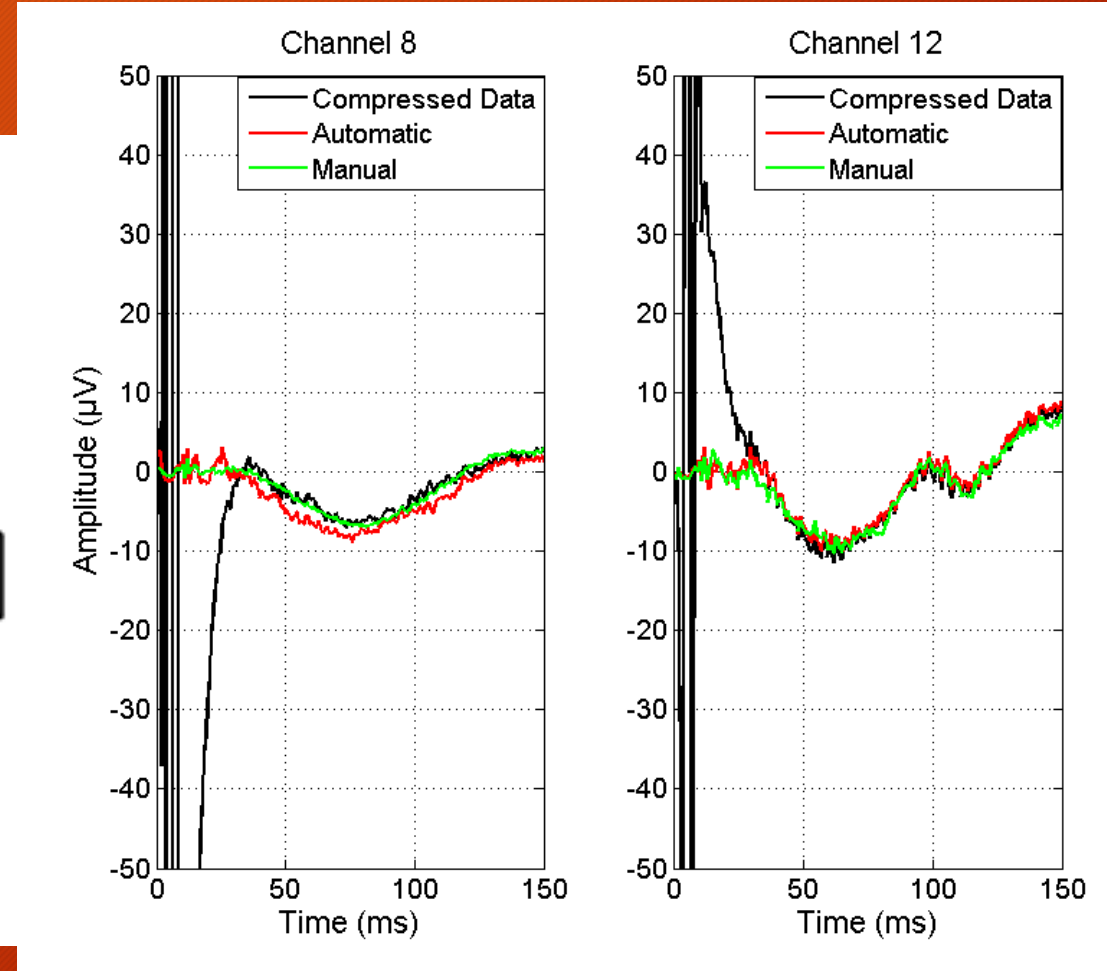
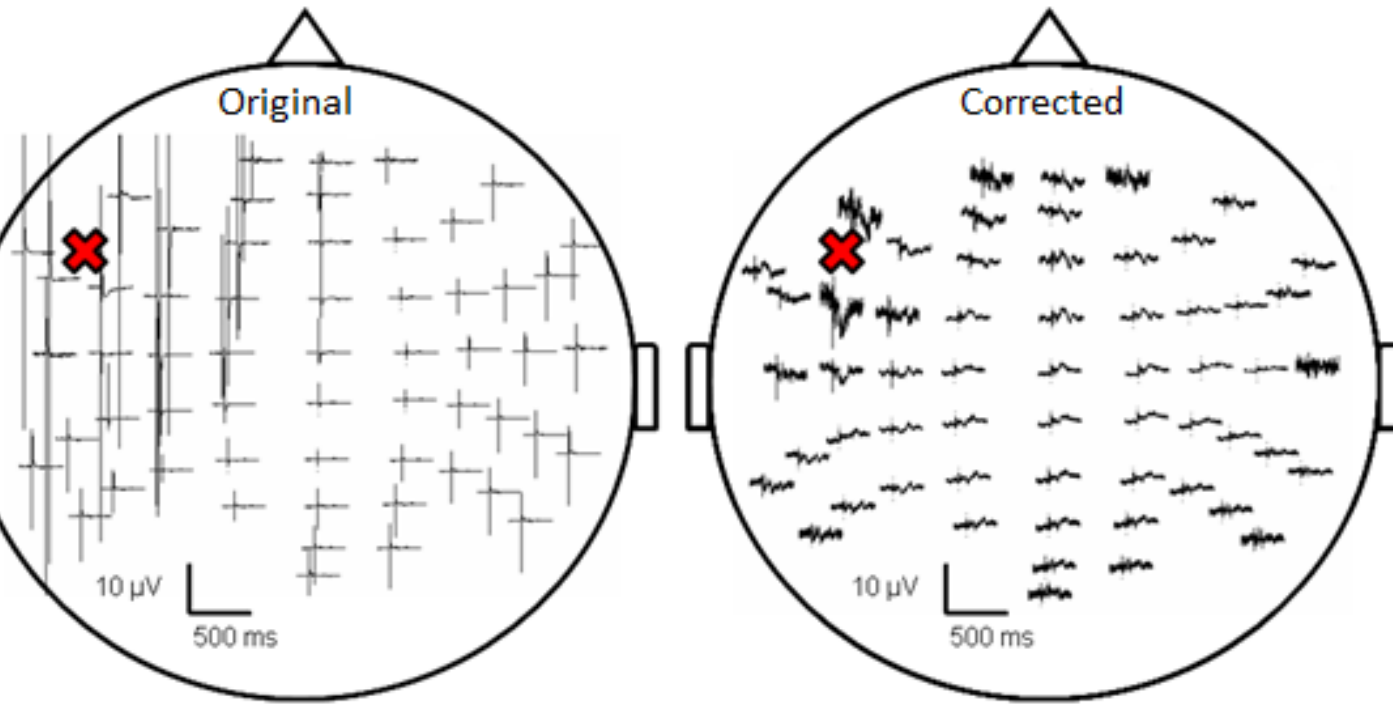


- Muscle artefact
- Topoplot
- High magnitude at 20-50 Hz
- Rule of thumb: If your're not sure whether artefact or not, leave it alone!



Removing muscle artifacts with ICA

$$\mathbf{X}_{\text{corr}} = \mathbf{X}_{\text{comp}} - \sum_{j=1}^p \hat{\mathbf{A}}(:, j) \hat{\mathbf{S}}(j, :)$$



ORIGINAL ARTICLE

Removal of large muscle artifacts from transcranial magnetic stimulation-evoked EEG by independent component analysis

**Reeta J. Korhonen · Julio C. Hernandez-Pavon ·
Johanna Metsomaa · Hanna Mäki ·
Risto J. Ilmoniemi · Jukka Sarvas**

Journal of Neuroscience Methods 209 (2012) 144–157



Contents lists available at SciVerse ScienceDirect

Journal of Neuroscience Methods

journal homepage: www.elsevier.com/locate/jneumeth



Computational Neuroscience

Uncovering neural independent components from highly artifactual TMS-evoked EEG data

Julio C. Hernandez-Pavon^{a,c,*}, Johanna Metsomaa^{a,b,1}, Tuomas Mutanen^{a,b}, Matti Stenroos^a,
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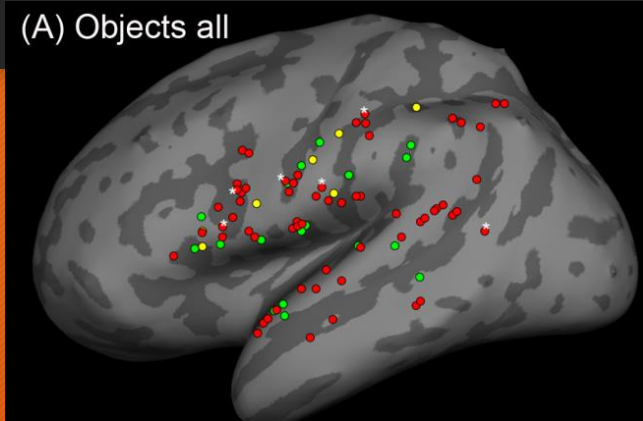
- The muscle artifacts distort the topographies.
- The topographies are useful in source localization.

Connectivity

- TMS-pulse
- After 3 ms activation structures close by are activated
- 20 ms the activation spreads on the opposite side

Summary

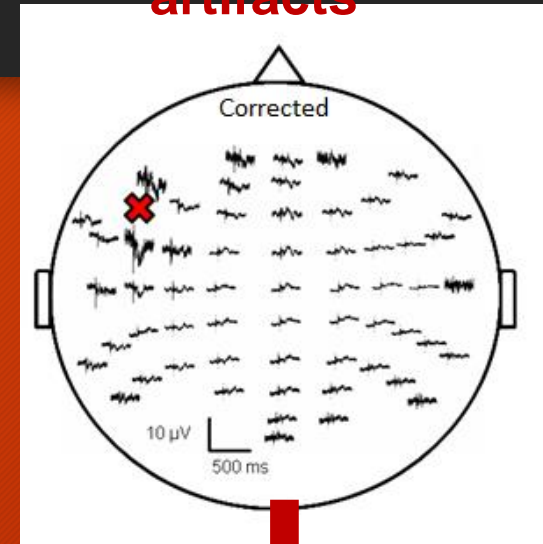
Functional localization of language areas



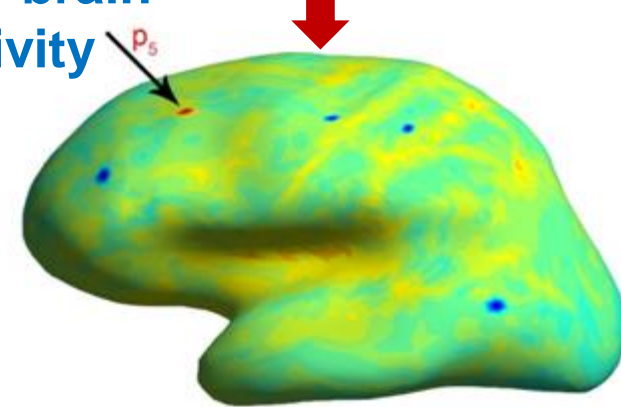
TMS-EEG



Methods for removing or Suppressing artifacts



Source localization to study brain connectivity



Basic Research

Clinical applications

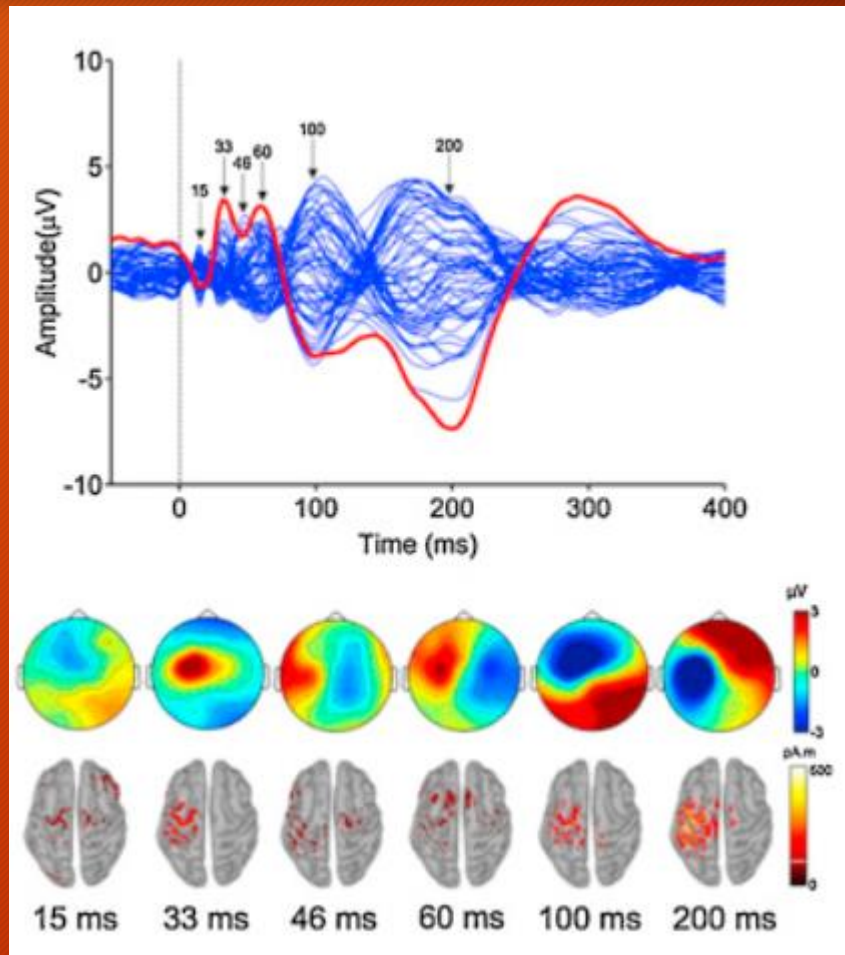


What was achieved?

- Highly artefactual (muscle activation) data was cleaned
- Brain topographies (voltage maps) at different time points after the TMS pulse are obtained
- Source localization estimates
- Dynamic information on the underlying brain activity

- Other possible applications include complexity measures that allow the evaluation of consciousness in unresponsive patients (vegetative, minimally conscious, locked-in?)

Example # 3 Source localization



Example # 3 Source localization

- The problem: We want to know which area inside the brain is creating certain signal, e.g. epileptic spike activity or evoked potential response to a stimulus
- Goal: 3D representation of the activated area within the brain

Source localization

Inverse problem:

” There are many possible dipole sources that can create the same voltage distribution measured on the scalp. Which is the correct distribution of sources?”

Forward problem describes how the known dipolar sources propagate to the scalp

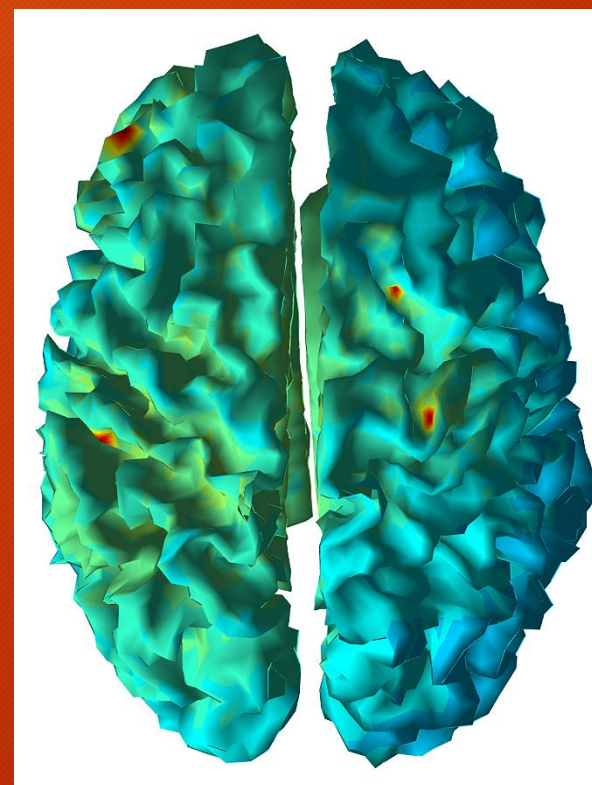
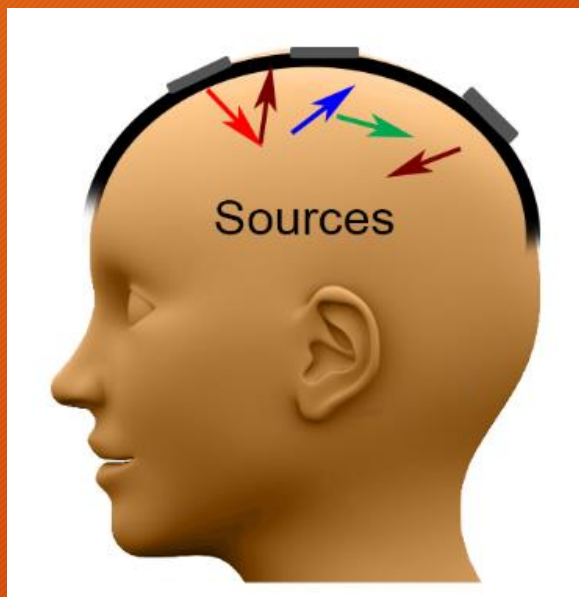
Inverse problem is much harder to solve. When the voltage distribution is known, it will give you estimation of the sources that created that distribution

Source localization

EEG



Brain sources



Beamformer

Source localization

- Spatial sampling density of EEG
- Head conductivity model
- Linear inverse weigh techniques to find the sources
- Matlab (Beamformer, EPIFOCUS, sLORETA)

Source localization, basic steps

MEG/EEG data analysis

MEG/EEG measurement

Signal processing

Improve signal-to-noise ratio of the signal components of interest, e.g., by averaging trials and by filtering.

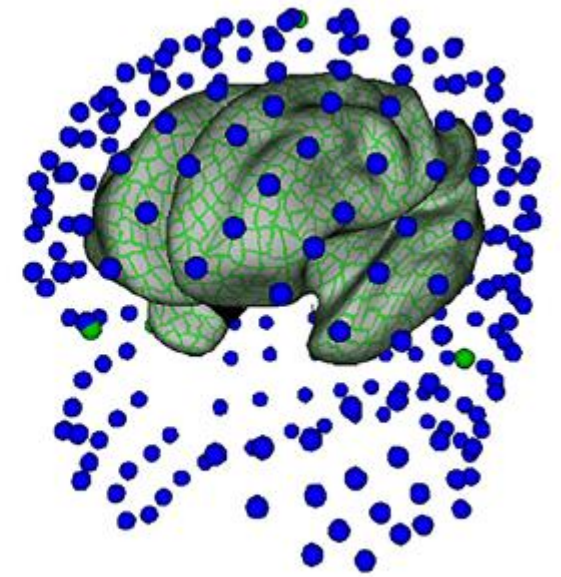
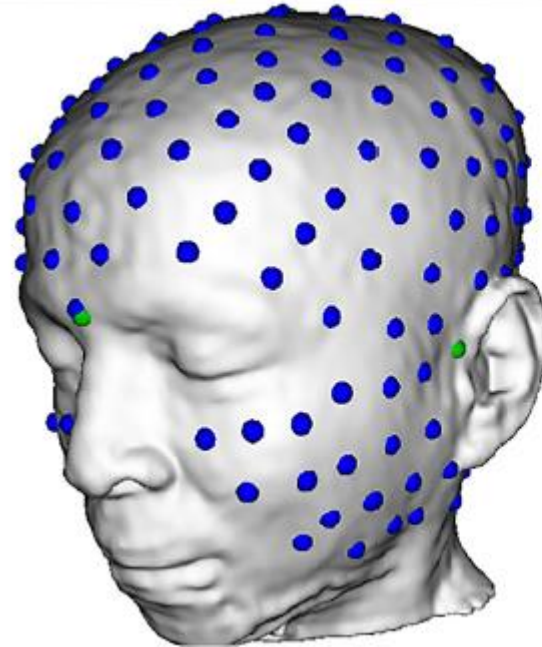
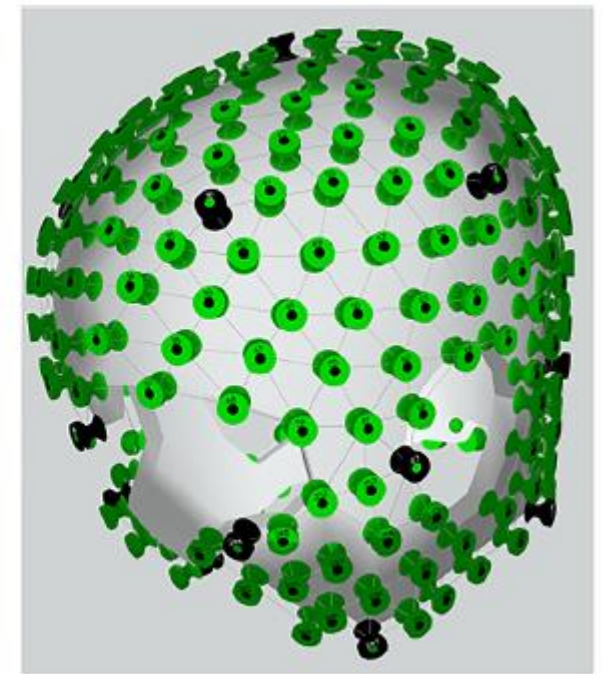
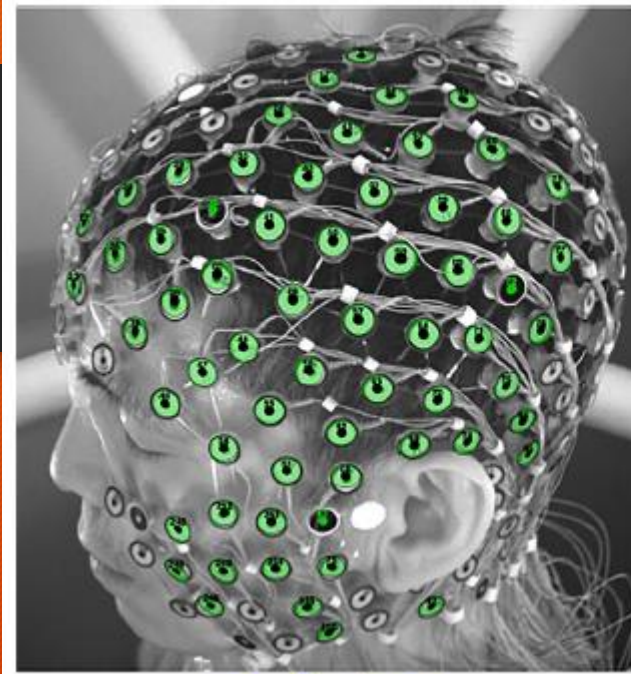
Source modelling

Estimate the primary current distribution (or its statistic) given the MEG/EEG data.

Visualization

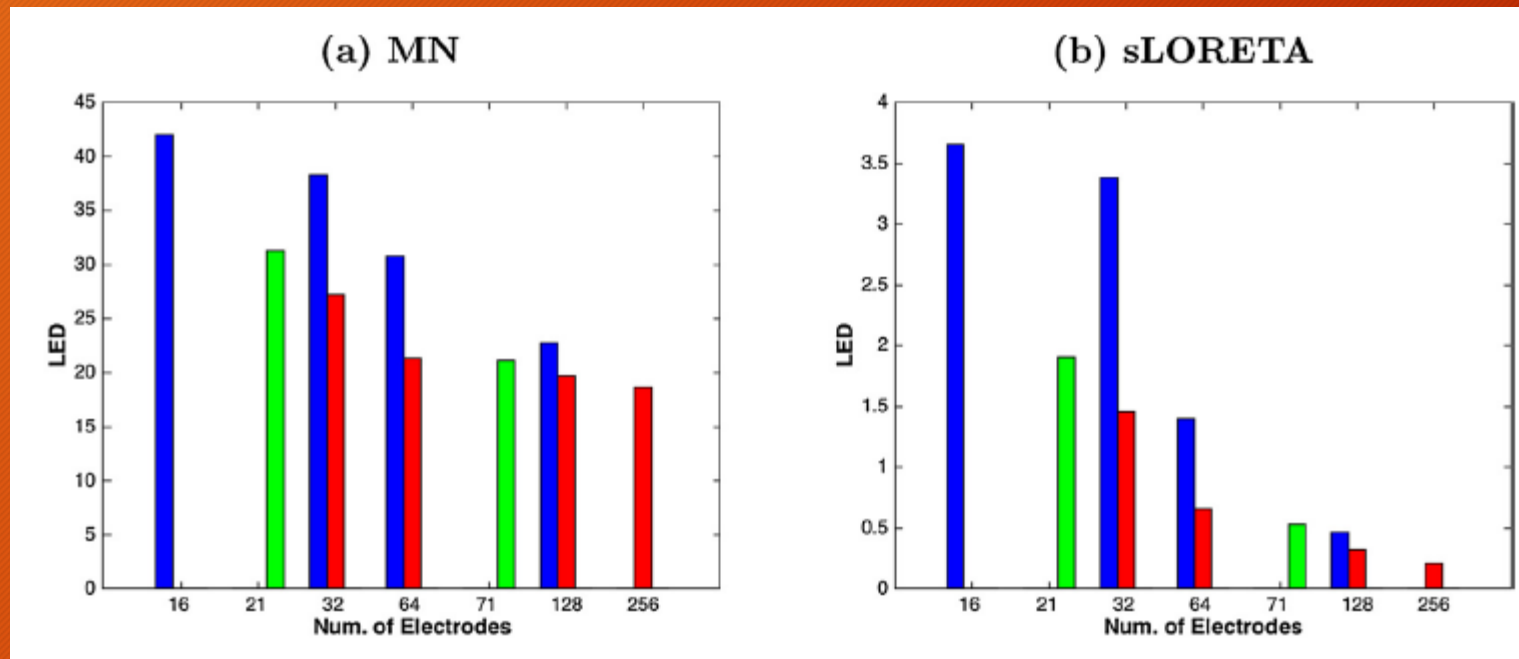
Superimpose the source estimate on the anatomical MR image

- Traditionally only scalp electrodes were used
- Additional data points from sampling the lower part of the head
- Realistic, individual head model



Spatial sampling

- Using simulated data, the effects of spatial sampling can be shown as Localization Error Distance



RED=whole head
Blue=upper head
Green= 10-20 system

Patient case

- Epileptic focus localized on the temporal region

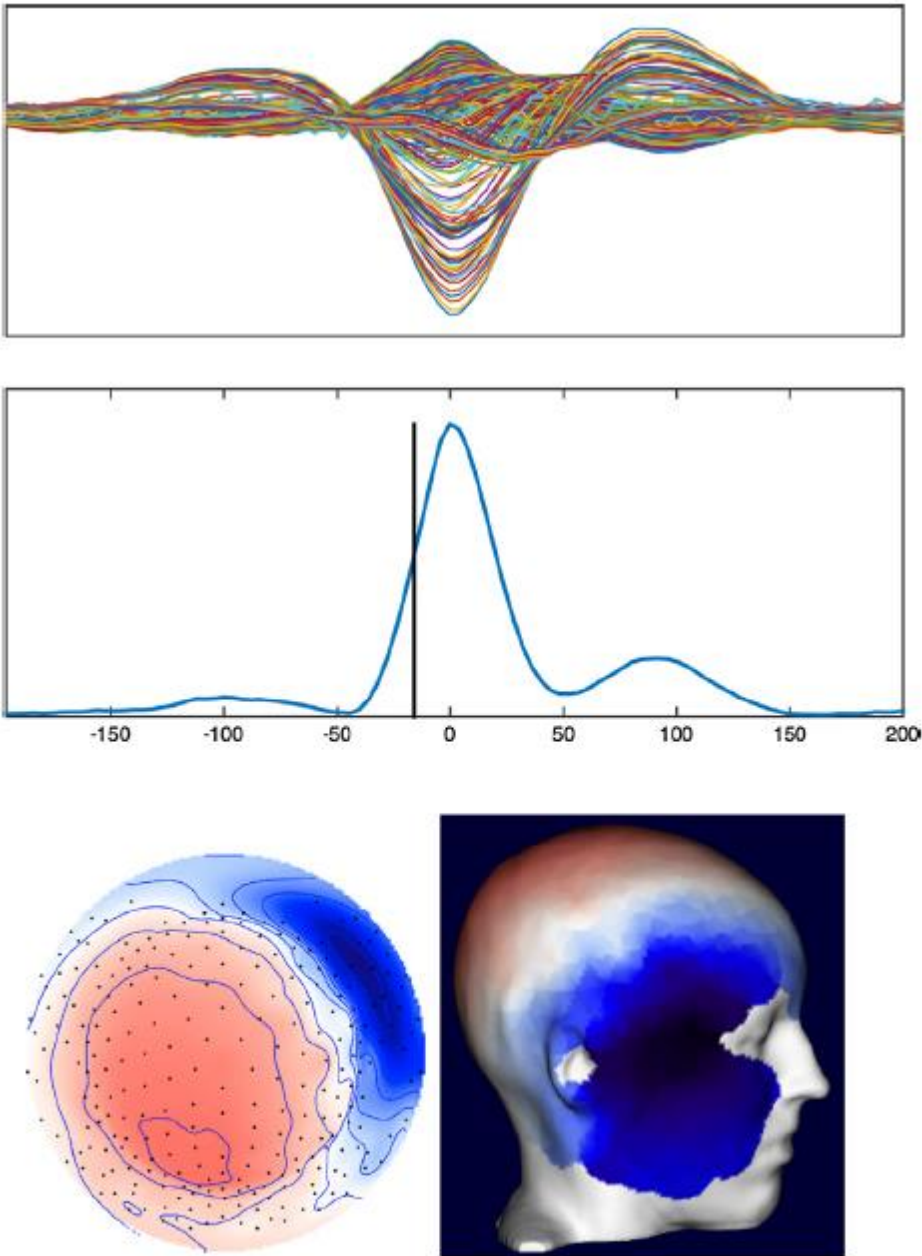


Fig. 7. Spike Onset localized in a patient's individual head model. (Top) 256-channel butterfly plot of average spike waveforms from -200 ms to 200 ms around spike peak and global field power. Black bar indicates time of spike onset used in source localization. (Bottom) Average spike scalp topography at onset.

(a) MN

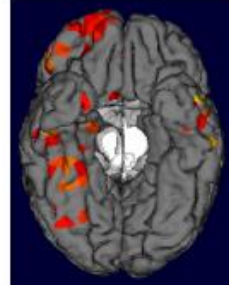
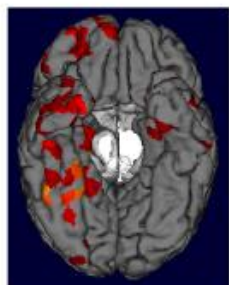
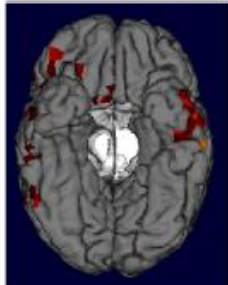
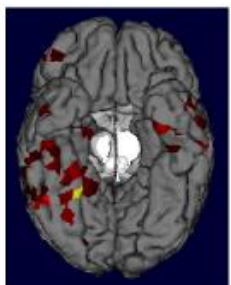
(b) sLORETA

whole 256

upper 128

whole 256

upper 128

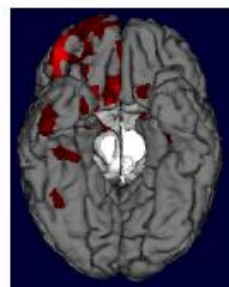
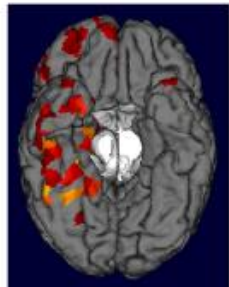
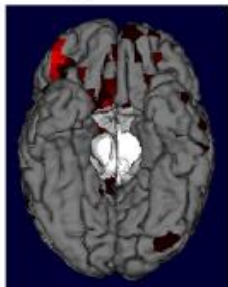
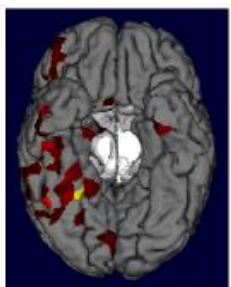


whole 128

upper 64

whole 128

upper 64

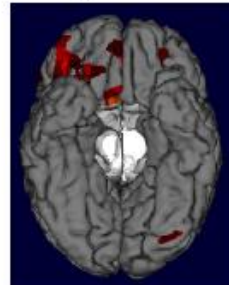
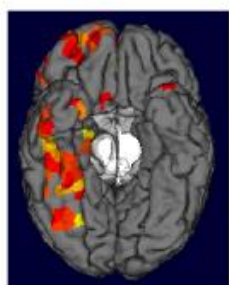
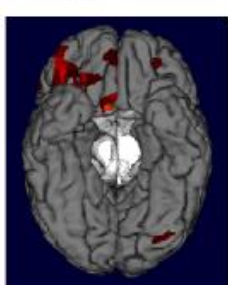
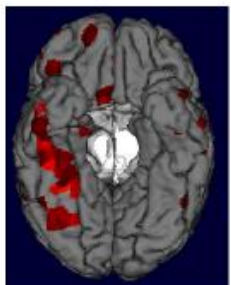


whole 64

upper 32

whole 64

upper 32

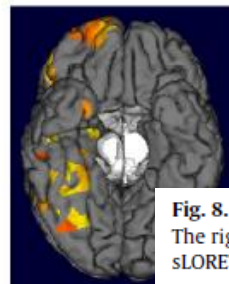
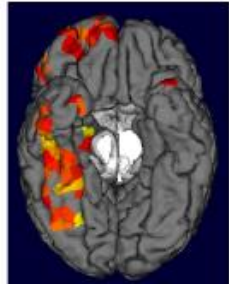
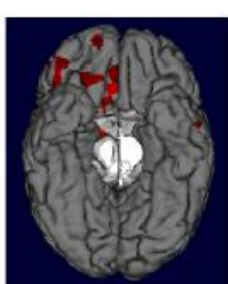
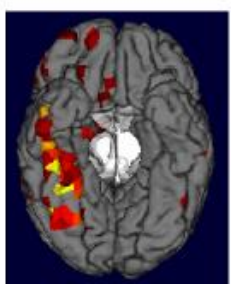


whole 32

upper 16

whole 32

upper 16



- Same patient as before, image showing the bottom of the brain
- Localizations look different with different spatial sampling
- Compare especially upper head vs. whole head (whole 128 vs upper 64)

Fig. 8. Spike Onset localized in a patient's individual head model with MN and sLORETA. (a) MN and (b) sLORETA source distributions with different sensor distributions. The right anterior temporal lobe was independently identified as the epileptogenic spike onset from intracranial data (and surgical outcome). Whole samples with MN and sLORETA are correctly localized.

Example #4 Brain Computer Interface

- Test subject generated patterns in brain signals are recognized and classified by a number of different methods
- <https://www.youtube.com/watch?v=7t84lGE5TXA>

Conclusions

- Several signal processing methods are available
- Matlab is a powerful tool and dedicated software packages are available
- Spectral distributions are excellent for visualizing large amounts of data
- Several approaches for removing noise (filtering, ICA, spectral properties of the signal)
- Signal processing techniques are being continually developed
- Also new applications emerge in clinical and for research purposes